

# Resolution of the $^{14}\text{N}$ Nuclear Quadrupole Hyperfine Structure in the Rotational Spectrum of Hydrazoic Acid, $\text{HN}_3$ , and Evaluation of the Rotational Constants of $\text{H}^{15}\text{NNN}$ and $\text{HNN}^{15}\text{N}$

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Z. Naturforsch. **44a**, 1079–1086 (1989); received August 12, 1989

Microwave Fourier transform spectra have been measured for hydrazoic acid as its normal isotopomer,  $\text{H}^{14}\text{N}_3$ , and two substituted isotopomers,  $\text{H}^{15}\text{N}^{14}\text{N}^{14}\text{N}$  and  $\text{H}^{14}\text{N}^{14}\text{N}^{15}\text{N}$ . The  $^{14}\text{N}$  quadrupole hyperfine structure has been resolved in all cases, and the quadrupole coupling constants of all  $^{14}\text{N}$  atoms have been determined. They are compared with those from *ab initio* predictions. Rotational constants  $A$  have been evaluated accurately for the first time for the two  $^{15}\text{N}$  species, and have been used to confirm a previously published structure.

## Introduction

Although the microwave spectrum of hydrazoic acid,  $\text{HN}_3$ , has been studied several times at both low and high frequencies, the hyperfine structure due to the three  $^{14}\text{N}$  nuclei has never been completely resolved. Traditional Stark modulated and millimeter wave spectrometers do not normally have the resolving power to achieve this. Thus, although several papers reported partial resolution of the hyperfine structure [1–3], values for only two of the six quadrupole coupling constants have been measured [1]. Since these constants have been the subject of several *ab initio* predictions [4, 5], an experimental determination of all of them is certainly of interest.

The relatively new technique of microwave Fourier transform (MWFT) spectroscopy has at least an order of magnitude better resolving power than the traditional methods. It has recently been extensively reviewed [6]. It should thus seem to be an excellent technique to resolve the  $^{14}\text{N}$  hyperfine structure in  $\text{HN}_3$ . We show in this paper that this is indeed the case, although the spectra are rather too complex for easy determination of the coupling constants.

Since the coupling patterns are very much simplified by replacing one  $^{14}\text{N}$  by  $^{15}\text{N}$  we have obtained the constants by instead measuring and analyzing the

MWFT spectra of the two substituted species  $\text{H}^{15}\text{N}^{14}\text{N}^{14}\text{N}$  and  $\text{H}^{14}\text{N}^{14}\text{N}^{15}\text{N}$ . Although microwave spectra of both have been previously reported [2] it is interesting that the only measured transitions were *a*-type R-branches, so that only two of the three rotational constants could be accurately determined. Only a crude value of the rotational constant  $A$  was obtained from  $K_a=2$  asymmetry splittings. More recently however, Winnewisser [7] suggested some improved values for  $A$  by transferring the inertial defect from the normal species,  $\text{H}^{14}\text{N}_3$ , which she then used in a structural determination. It was thus a second goal of the present work to locate and measure some *b*-type transitions of these species in order to obtain accurate values for  $A$ .

## Experimental Methods

The samples of  $\text{HN}_3$  were prepared by gently heating dry sodium azide with stearic acid. The labelled species were obtained in equal amounts in a similar preparation, which this time used  $\text{NaN}^{15}\text{N}$  (99%  $^{15}\text{N}$ , ICN Biochemicals). Because of the well known explosive nature of hydrazoic acid, the samples were stored in milligram quantities below 100 Torr in the gas phase in the dark at room temperature. They were apparently stable enough for the purpose of these experiments.

The spectra were measured using the MWFT travelling wave spectrometers in G- [8], K- [9] and V- [10] band at the University of Kiel. Sample pressures were below 2 mTorr ( $<0.3$  Pa), and temperatures were

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about 200 K. Up to  $40 \cdot 10^6$  cycles were collected for individual transitions, covering averaging times up to one half hour. Although the spectra were displayed by taking the fast Fourier transforms of the decay signals, accurate frequencies were obtained by fitting the decays in the time domain, using the program developed by Haekel and Mäder [11].

### Observed Spectrum and Assignment

The first transition observed was  $1_{01} - 0_{00}$ , in K-band, which Forman and Lide could resolve only partially [1]. For all three isotopic species studied the quadrupole hyperfine structure of all  $^{14}\text{N}$  nuclei was resolved. The observed lines are depicted in Fig. 1(a), (c) and (d).

Because only the coupling constants  $\chi_{aa}$  could be determined with the  $1_{01} - 0_{00}$  transition, it was necessary to make further measurements, especially of  $a$ -type Q-branch transitions, to evaluate  $\chi_{bb} - \chi_{cc}$ . For the normal isotope they were predicted from the observations of Bendtsen and Winnewisser [3], who had previously measured some of these. For the substituted species they were predicted from the rotational constants of Winnewisser and Cook [2]. In all cases the transitions were easily located. Their assignments were confirmed with the hyperfine structure.

To evaluate the rotational constant  $A$  for  $\text{H}^{15}\text{NNN}$  and  $\text{HNN}^{15}\text{N}$  some  $b$ -type lines had to be found. Because this constant was expected to be very large ( $\sim 600$  GHz) only one P, R-branch series had transitions in our frequency region. These lines were potentially very difficult to find by estimating  $A$  from a structure because the uncertainties could have been thousands of MHz. Fortunately the estimates made by Winnewisser [7] reduced the uncertainties to  $\pm 300$  MHz, which was relatively manageable, especially since these transitions were expected to be strong. All of them were found within this region; the assignments were again confirmed with the hyperfine structure.

### Analysis of the Spectrum

To start the analysis, the  $^{14}\text{N}$  quadrupole coupling constants were evaluated for each of the labelled species. From a prediction using crude estimates of the constants from the spectrum, quantum number as-

Table 1. Derived spectroscopic constants of  $\text{H}^{15}\text{N}^{14}\text{N}^{14}\text{N}$  and  $\text{H}^{14}\text{N}^{14}\text{N}^{15}\text{N}$ .

Parameter	$\text{H}^{15}\text{N}^{14}\text{N}^{14}\text{N}$	$\text{H}^{14}\text{N}^{14}\text{N}^{15}\text{N}$
Rotational constants (MHz)		
$A$	605 583.30 (15)	610 979.7 (2)
$B$	11 667.5433 (15)	11 641.7764 (14)
$C$	11 427.8558 (15)	11 405.0788 (14)
Centrifugal distortion constants (kHz)		
$D_J$	4.627 (5)	4.540 (5)
$D_{JK}$	769.0 (8)	752.3 (8)
$D_K$	270 480.0 <sup>b</sup>	270 480.0 <sup>b</sup>
$d_1$	-0.0836 (15)	-0.0827 (15)
$d_2$	-0.023 (14)	-0.027 (13)
$10^4 H_{JK}$	9.32 <sup>b</sup>	9.32 <sup>b</sup>
$H_{KJ}$	-0.07 (11)	-0.25 (12)
$H_K$	520.0 <sup>b</sup>	520.0 <sup>b</sup>
$^{14}\text{N}$ nuclear quadrupole coupling constants (MHz)		
$\text{N}_\alpha$	$\chi_{aa}$ —	4.727 (5)
	$\chi_{bb} - \chi_{cc}$ —	2.271 (3)
$\text{N}_\beta$	$\chi_{aa}$ -0.819 (17)	-0.858 (8)
	$\chi_{bb} - \chi_{cc}$ 0.209 (4)	0.197 (4)
$\text{N}_\gamma$	$\chi_{aa}$ -1.224 (14)	—
	$\chi_{bb} - \chi_{cc}$ 3.998 (4)	—

<sup>a</sup> Numbers in parentheses are one standard deviation obtained in the least squares fit, in units of the last significant figures.

<sup>b</sup> These constants were held fixed in the least squares fit at the values for  $\text{H}^{14}\text{N}_3$  [14].

<sup>c</sup> The notation refers to the N atoms in the order  $\text{HN}_\alpha\text{N}_\beta\text{N}_\gamma$ .

signments were made in the coupling schemes  $I_1 + I_2 \rightarrow I$ ,  $I + J \rightarrow F$  as well as in the alternative scheme  $J + I_1 \rightarrow F_1$ ,  $F_1 + I_2 \rightarrow F$ . A least squares fit was then made to the quadrupole coupling constants using a program written by Böttcher [12]; it fitted shifts of the lines from the unsplit line frequency, and in the process calculated that frequency. The program used a full diagonalization of the Hamiltonian, including terms off-diagonal in  $I$  but not  $J$ . This is well known to be sufficient for the small coupling constants found here. Well resolved lines of the  $a$ -type R-branch and several Q-branch transitions were included in the fit. The rotational constants  $B$  and  $C$  were taken from [2], and  $A$  was estimated from the observed  $b$ -type transitions.

The results of these fits are given in Table 1. Since both labelled species contain  $^{14}\text{N}$  at the central position of the azide group, the values common to both isotopomers were assigned to this nucleus ( $\text{N}_\beta$ ). The others were assigned to the unsubstituted nucleus. The agreement between the values obtained for  $\text{N}_\beta$  is reasonable (within 2 standard deviations).

Table 2. Observed rotational transitions (MHz) of  $\text{H}^{15}\text{N}^{14}\text{N}^{14}\text{N}$ .

$F'_1$	$F'$	$F''_1$	$F''$	Observed Line		$F'_1$	$F'$	$F''_1$	$F''$	Observed Line	
				Frequency	Dev. <sup>a</sup>					Frequency	Dev. <sup>a</sup>
$1_{0,1}-0_{0,0}$				23 095.381 <sup>b</sup>	0.000	$13_{1,12}-13_{1,13}$				21 805.917 <sup>b</sup>	-0.001
1	0	1	— <sup>c</sup>	23 094.865	-0.006	13	13	13	13	21 804.854	0.000
1	2	1	—	23 095.011	-0.004	13	13	12	13	21 804.940	0.004 <sup>d</sup>
1	1	1	—	23 095.059	-0.003	13	14	13	14	21 804.940	0.000
2	2	1	—	23 095.388	-0.001	13	12	13	12	21 804.940	-0.005
2	3	1	—	23 095.487	0.004	14	14	14	14	21 806.314	0.000
2	1	1	—	23 095.623	0.000	14	15	14	15	21 806.386	-0.002 <sup>d</sup>
0	1	1	—	23 096.066	-0.006	14	13	14	13	21 806.386	-0.017 <sup>d</sup>
$6_{1,5}-6_{1,6}$				5 033.140 <sup>b</sup>	0.001	12	12	12	12	21 806.430	0.003
6	6	6	6	5 032.064	0.001	12	11	12	11	21 806.505	-0.001
6	7	6	7	5 032.154	-0.001 <sup>d</sup>	12	13	12	13	21 806.505	-0.001
6	7	7	6	5 032.154	-0.002	$17_{1,16}-17_{1,17}$				36 656.018 <sup>b</sup>	0.001
6	5	6	5	5 032.164	-0.001	17	17	17	17	36 654.962	0.006
6	6	5	6	5 032.242	-0.002 <sup>d</sup>	17	18	17	18	36 655.044	0.002
7	7	7	7	5 033.496	0.002	17	16	17	16	36 655.044	-0.002
7	6	6	6	5 033.496	0.002	18	18	18	18	36 656.428	0.002
7	8	7	8	5 033.559	-0.002	18	19	18	19	36 656.505	0.004
7	6	7	6	5 033.587	-0.002	18	17	18	17	36 656.505	-0.007
5	6	7	6	5 033.736	0.011	16	16	16	16	36 656.505	-0.007
5	5	5	5	5 033.736	0.003	16	17	16	17	36 656.593	0.001
5	6	5	6	5 033.811	0.003	16	15	16	15	36 656.593	0.001
5	4	5	4	5 033.811	0.001	$22_{1,22}-23_{0,23}$				32 836.862 <sup>b</sup>	0.001
$7_{1,6}-7_{1,7}$				6 710.722 <sup>b</sup>	0.000	22	23	21	22	32 836.585	-0.005 <sup>d</sup>
7	7	7	7	6 709.647	0.001	22	21	21	20	32 836.585	-0.006 <sup>d</sup>
7	7	8	7	6 709.725	-0.001	24	23	23	22	32 836.621	0.002 <sup>d</sup>
7	8	7	8	6 709.741	0.002	24	25	23	24	32 836.621	-0.003 <sup>d</sup>
7	6	7	6	6 709.747	-0.001	22	22	21	21	32 836.621	-0.009 <sup>d</sup>
7	7	6	7	6 709.795	0.002 <sup>d</sup>	24	24	23	23	32 836.656	-0.005 <sup>d</sup>
8	8	8	8	6 711.086	0.000	23	22	22	21	32 837.335	0.005 <sup>d</sup>
8	7	7	7	6 711.097	-0.003	23	24	22	23	32 837.335	0.004 <sup>d</sup>
8	9	8	9	6 711.153	-0.002	23	23	22	22	32 837.379	0.004 <sup>d</sup>
8	7	8	7	6 711.178	-0.003	$23_{1,23}-24_{0,24}$				7 114.989 <sup>b</sup>	-0.002
6	6	6	6	6 711.295	0.003	23	24	22	23	7 114.718	-0.001 <sup>d</sup>
6	7	8	7	6 711.295	-0.002	23	22	22	21	7 114.718	-0.003 <sup>d</sup>
6	7	6	7	6 711.370	0.002	23	23	22	22	7 114.753	-0.006 <sup>d</sup>
6	5	6	5	6 711.370	0.001	23	24	24	23	7 114.753	0.009 <sup>d</sup>
$12_{1,11}-12_{1,12}$				18 691.488 <sup>b</sup>	0.000	25	24	24	23	7 114.753	0.006 <sup>d</sup>
12	12	12	12	18 690.423	0.003	25	26	24	25	7 114.753	0.002 <sup>d</sup>
12	12	13	12	18 690.488	0.019	25	24	23	23	7 114.792	0.008 <sup>d</sup>
12	13	12	13	18 690.514	0.004	25	25	24	24	7 114.792	0.003 <sup>d</sup>
12	12	11	12	18 690.514	0.003 <sup>d</sup>	24	23	23	22	7 115.455	0.000 <sup>d</sup>
12	11	12	11	18 690.514	-0.002	24	25	23	24	7 115.455	-0.001 <sup>d</sup>
13	13	13	13	18 691.876	-0.010	24	24	24	23	7 115.455	-0.008 <sup>d</sup>
13	12	12	12	18 691.922	0.000	24	24	23	23	7 115.497	-0.003 <sup>d</sup>
13	14	13	14	18 691.957	0.002 <sup>d</sup>	$25_{0,25}-24_{1,24}$				18 708.263 <sup>b</sup>	-0.001
13	12	13	12	18 691.957	-0.014 <sup>d</sup>	25	25	24	24	18 707.756	0.001 <sup>d</sup>
11	11	11	11	18 692.006	0.003	25	26	24	25	18 707.797	-0.001 <sup>d</sup>
11	12	13	12	18 692.040	-0.001	25	24	24	23	18 707.797	-0.002 <sup>d</sup>
11	10	11	10	18 692.083	0.000	26	26	25	25	18 708.464	0.001 <sup>d</sup>
11	12	11	12	18 692.083	0.000	26	25	24	24	18 708.464	-0.008 <sup>d</sup>
						24	24	23	23	18 708.497	0.006 <sup>d</sup>
						26	27	25	26	18 708.497	-0.002 <sup>d</sup>
						26	25	25	24	18 708.497	-0.007 <sup>d</sup>
						24	23	23	22	18 708.531	0.002 <sup>d</sup>
						24	25	23	24	18 708.531	0.001 <sup>d</sup>

<sup>a</sup> For the unsplit line this is the “observed” unsplit frequency minus that calculated from the derived rotational and centrifugal distortion constants. For the hyperfine components this is the observed frequency minus that calculated from the derived quadrupole coupling constants and centre frequencies.

<sup>b</sup> Unsplit line frequency calculated from the measured frequencies corrected for hyperfine structure.

<sup>c</sup>  $F''=0, 1$  or  $2$ ; all levels with  $J=0$  are degenerate.

<sup>d</sup> These transitions were not included in the least squares fit for the quadrupole coupling constants.

Table 3. Observed rotational transitions (MHz) of  $\text{H}^{14}\text{N}^{14}\text{N}^{15}\text{N}$ .

$F'_1$	$F'$	$F''_1$	$F''$	Observed Line		$F'_1$	$F'$	$F''_1$	$F''$	Observed Line	
				Frequency	Dev. <sup>a</sup>					Frequency	Dev. <sup>a</sup>
$1_{0,1} - 0_{0,0}$				23 046.838 <sup>b</sup>	0.001	$14_{1,13} - 14_{1,14}$				24 845.806 <sup>b</sup>	0.001
0	1	1	— <sup>c</sup>	23 044.453	−0.005	14	14	14	14	24 845.188	−0.003
2	1	1	—	23 046.443	0.000	14	15	14	15	24 845.263	0.002
2	3	1	—	23 046.646	0.002	14	13	14	13	24 845.263	−0.003
2	2	1	—	23 046.718	0.006	15	15	15	15	24 846.016	0.002
1	0	1	—	23 047.804	−0.001	15	14	15	14	24 846.087	0.015 <sup>d</sup>
1	2	1	—	23 048.006	0.000	13	13	13	13	24 846.087	0.003 <sup>d</sup>
1	1	1	—	23 048.165	−0.006	15	16	15	16	24 846.087	0.000 <sup>d</sup>
$6_{1,5} - 6_{1,6}$				4 970.358 <sup>b</sup>	0.000	13	14	13	14	24 846.146	0.003
6	6	6	6	4 969.748	−0.001	13	12	13	12	24 846.146	−0.003
6	7	6	7	4 969.810	0.000	$17_{1,16} - 17_{1,17}$				36 198.776 <sup>b</sup>	0.000
6	5	6	5	4 969.821	0.000	17	17	17	17	36 198.157	−0.003
7	7	7	7	4 970.536	0.000	17	18	17	18	36 198.232	0.001
7	8	7	8	4 970.610	−0.002	17	16	17	16	36 198.232	−0.003
7	6	7	6	4 970.610	−0.002	18	18	18	18	36 198.991	0.004
5	5	5	5	4 970.668	−0.003 <sup>d</sup>	16	16	16	16	36 199.076	0.040 <sup>d</sup>
5	6	5	6	4 970.731	−0.005	18	19	18	19	36 199.076	0.017 <sup>d</sup>
5	4	5	4	4 970.748	−0.003	18	17	18	17	36 199.076	0.013 <sup>d</sup>
$7_{1,6} - 7_{1,7}$				6 627.012 <sup>b</sup>	−0.001	16	17	16	17	36 199.076	−0.032 <sup>d</sup>
7	7	7	7	6 626.400	−0.001	16	15	16	15	36 199.076	−0.036 <sup>d</sup>
7	8	7	8	6 626.466	0.001	$22_{1,22} - 23_{0,23}$				39 731.657 <sup>b</sup>	0.000
7	6	7	6	6 626.477	0.002	21	20	22	21	39 731.524	0.024 <sup>d</sup>
8	8	8	8	6 627.197	0.000	21	22	22	23	39 731.524	0.022 <sup>d</sup>
8	9	8	9	6 627.271	0.004	23	22	24	23	39 731.524	0.002 <sup>d</sup>
8	7	8	7	6 627.271	−0.002	23	24	24	25	39 731.524	0.001 <sup>d</sup>
6	6	6	6	6 627.311	−0.002 <sup>d</sup>	21	21	22	22	39 731.524	−0.014 <sup>d</sup>
6	7	6	7	6 627.374	−0.006	24	24	23	23	39 731.524	−0.035 <sup>d</sup>
6	5	6	5	6 627.391	−0.001	22	21	23	22	39 731.922	0.013 <sup>d</sup>
$12_{1,11} - 12_{1,12}$				18 458.329 <sup>b</sup>	0.000	22	23	23	24	39 731.922	0.012 <sup>d</sup>
12	12	12	12	18 457.712	−0.002	22	22	23	23	39 731.922	−0.025 <sup>d</sup>
12	13	12	13	18 457.786	0.003	$26_{0,26} - 25_{1,25}$				37 497.890 <sup>b</sup>	0.000
12	11	12	11	18 457.786	−0.003	26	26	25	25	37 497.625	0.022 <sup>d</sup>
13	13	13	13	18 458.533	0.001	26	27	25	26	37 497.625	−0.013 <sup>d</sup>
13	12	13	12	18 458.606	0.004 <sup>d</sup>	26	25	25	24	37 497.625	−0.014 <sup>d</sup>
11	11	11	11	18 458.606	0.003 <sup>d</sup>	27	27	26	26	37 498.024	0.036 <sup>d</sup>
13	14	13	14	18 458.606	−0.002 <sup>d</sup>	25	25	24	24	37 498.024	0.017 <sup>d</sup>
11	12	11	12	18 458.673	0.002	27	28	26	27	37 498.024	−0.001 <sup>d</sup>
11	10	11	10	18 458.673	−0.005	27	26	26	25	37 498.024	−0.002 <sup>d</sup>
$13_{1,12} - 13_{1,13}$				21 533.909 <sup>b</sup>	0.002	25	26	24	25	37 498.024	−0.019 <sup>d</sup>
13	13	13	13	21 533.292	−0.002	25	24	24	23	37 498.024	−0.020 <sup>d</sup>
13	14	13	14	21 533.366	0.002						
13	12	13	12	21 533.366	−0.003						
14	14	14	14	21 534.116	0.001						
14	13	14	13	21 534.187	0.009 <sup>d</sup>						
12	12	12	12	21 534.187	0.002 <sup>d</sup>						
14	15	14	15	21 534.187	−0.003 <sup>d</sup>						
12	13	12	13	21 534.251	0.003						
12	11	12	11	21 534.251	−0.004						

<sup>a</sup> For the unsplit line this is the “observed” unsplit frequency minus that calculated from the derived rotational and centrifugal distortion constants. For the hyperfine components this is the observed frequency minus that calculated from the derived quadrupole coupling constants and centre frequencies.

<sup>b</sup> Unsplit line frequency calculated from the measured frequencies corrected for hyperfine structure.

<sup>c</sup>  $F'' = 0, 1$  or  $2$ ; all levels with  $J = 0$  are degenerate.

<sup>d</sup> These transitions were not included in the least squares fit for the quadrupole coupling constants.

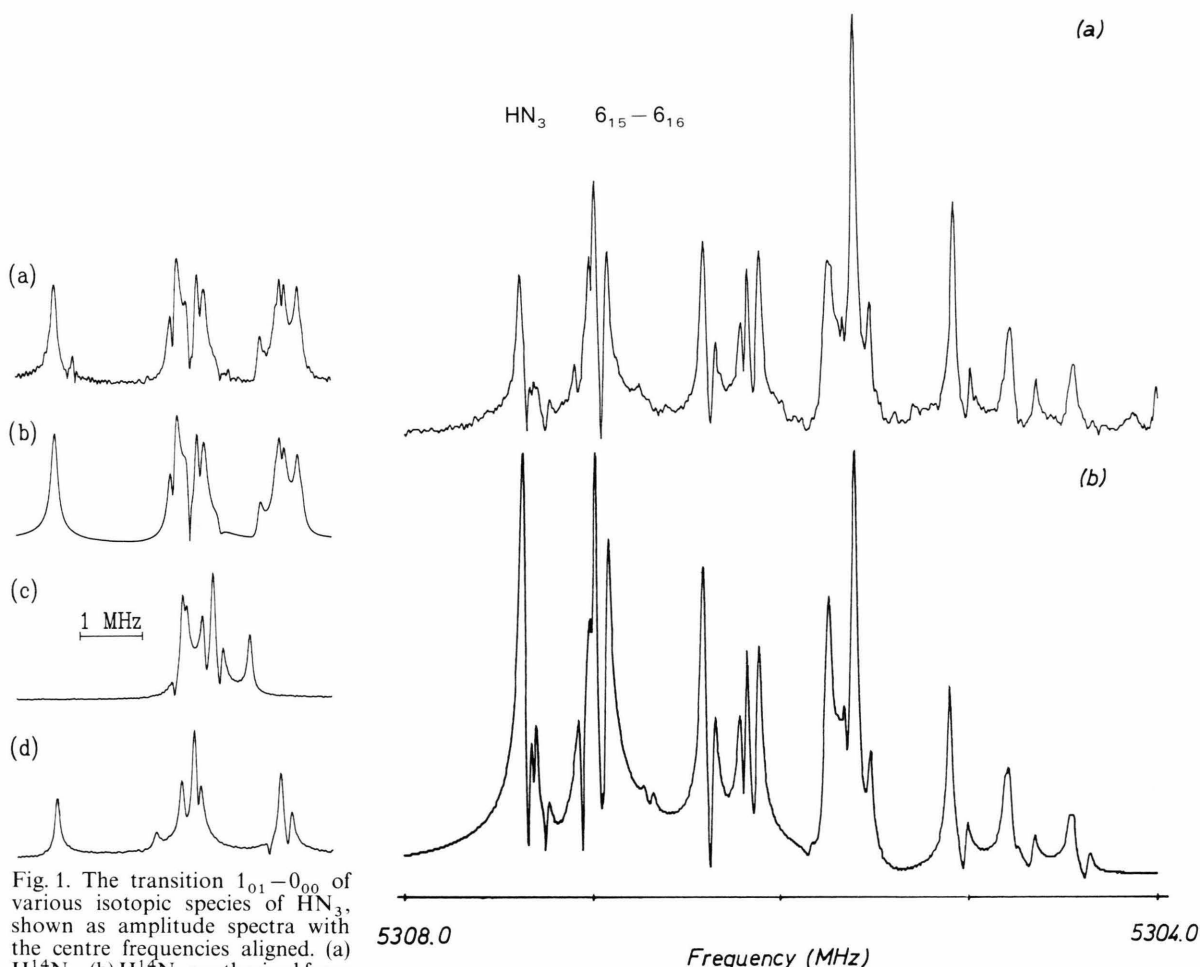


Fig. 1. The transition  $1_{01}-0_{00}$  of various isotopic species of  $\text{HN}_3$ , shown as amplitude spectra with the centre frequencies aligned. (a)  $\text{H}^{14}\text{N}_3$ , (b)  $\text{H}^{14}\text{N}_3$  synthesized from the observed constants and an assumed linewidth, (c)  $\text{H}^{15}\text{N}^{14}\text{N}^{14}\text{N}$ , (d)  $\text{H}^{14}\text{N}^{14}\text{N}^{15}\text{N}$ .

Fig. 2. The transition  $6_{15}-6_{16}$  of  $\text{H}^{14}\text{N}_3$ . In (a) the experimental amplitude spectrum is shown. In (b) the amplitude spectrum synthesized from the derived constants and an assumed linewidth is given.

The rotational and centrifugal distortion constants for the two labelled species were then obtained by a least squares fit. The frequencies used were the unsplit line frequencies (with the hyperfine structure subtracted off) of the transitions measured here, along with the corresponding measurements with  $K_a \leq 3$  in [2]. The data were weighted in inverse proportion to their estimated experimental uncertainty. The model followed the S-reduction Hamiltonian [13] of Cheung and Merer [14] used for the normal isotopic species. This in turn was similar to one introduced earlier to account for the microwave spectrum of isoelectronic  $\text{HNCO}$  [15]. Because we could observe only one  $b$ -type branch it was necessary to fix values of several

constants, namely  $D_K$ ,  $H_K$  and  $H_{JK}$  to the values of  $\text{H}^{14}\text{N}_3$  [14].

The results of the fits are in Table 1. Good values of the rotational constants,  $D_J$ ,  $D_{JK}$  and  $d_1$ , have been obtained. The rotational constants  $B$  and  $C$  are in good agreement with those of [2]. The distortion constants  $d_2$  and  $H_{KJ}$  are barely determined, if that. They were retained as fitting parameters for consistency with earlier work [15], and because the standard deviation of the fit deteriorated if they were omitted.

Tables 2 and 3 contain all the transition frequencies measured here for  $\text{H}^{15}\text{N}^{14}\text{N}^{14}\text{N}$  and  $\text{H}^{14}\text{N}^{14}\text{N}^{15}\text{N}$ , respectively. Because for both of these isotopomers one set of quadrupole coupling constants was bigger



Table 4. Frequencies and assignments of the  $1_{0,1}-0_{0,0}$  rotational transition of  $\text{H}^{14}\text{N}_3$ .

$F_1'$	$F_2'$	$F''^a$	Frequency (MHz)	
			Observed	Dev. <sup>b</sup>
$1_{0,1}-0_{0,0}$			23 815.631 <sup>c</sup>	
0	1	0	23 813.222	0.039
0	1	2	23 813.222	0.006
0	1	1	23 813.222	-0.016
2	2	2	23 815.076	0.000
2	2	3	23 815.154	0.007
2	2	1	23 815.154	-0.016
2	3	3	23 815.352	0.000
2	1	1	23 815.417	-0.003
2	3	4	23 815.504	0.006
2	3	2	23 815.573	0.017
2	1	2	23 815.573	-0.016
2	1	0	23 815.815	-0.017
1	0	1	23 816.466	0.001
1	2	1	23 816.746	-0.002
1	2	3	23 816.795	0.003
1	2	2	23 816.851	0.002
1	1	0	23 817.097	0.015
1	1	2	23 817.097	-0.004
1	1	1	23.817.140	-0.003

<sup>a</sup> Only the quantum numbers of the  $1_{0,1}$  level are given. For the  $0_{0,0}$  level  $F_1''=1$ ,  $F_2''=2, 1, 0$  and  $F''=3, 2, 1, 0$ ; all these levels are degenerate.

<sup>b</sup> Observed frequency minus that calculated using the derived constants and centre frequencies.

<sup>c</sup> Unsplit line frequency calculated from the measured frequencies corrected for the hyperfine structure.

than the other, the quantum numbers are given in the coupling scheme  $I_1+J \rightarrow F_1$ ,  $F_1+I_2 \rightarrow F$ . The excellence of the fit is clearly demonstrated by the small values of the deviations.

The quadrupole hyperfine patterns of  $\text{H}^{14}\text{N}_3$  were then predicted using the derived quadrupole constants. For  $\text{N}_\beta$ , the central N atom, the averages of the values in Table 1 were used. The calculation used a multinuclei program written originally by Cook [16], and adapted in Kiel to this project. The program was written in the coupling scheme  $J+I_1 \rightarrow F_1$ ,  $F_1+I_2 \rightarrow F_2$ ,  $F_2+I_3 \rightarrow F$ ; it included off-diagonal terms in the quantum numbers  $F_1$  and  $F_2$ , but not  $J$ .

The measured frequencies of the  $1_{01}-0_{00}$  transition of  $\text{H}^{14}\text{N}_3$  are given in Table 4. Quantum numbers are assigned in the scheme described above, with the assignments  $I_1=I_x$ ,  $I_2=I_y$  and  $I_3=I_\beta$ . The table also shows the deviations between the observed and calculated frequencies, and it is clear from them that the prediction is excellent. Figures 1(a) and (b) show a

comparison of the observed pattern with the calculated one; the agreement is again apparent.

Because the pattern for  $1_{01}-0_{00}$  depends only on  $\chi_{aa}$ , the patterns of the Q-branches were also predicted, in order to check the values for  $\chi_{bb}-\chi_{cc}$ . One such pattern, that of  $6_{15}-6_{16}$ , is given in Figure 2. The agreement between the observed and calculated patterns is rather good, and provides confirmation of the derived constants. Because the patterns are so complex, no attempt was made to compare observed and calculated frequencies.

## Discussion

This work has demonstrated, once again, the very high resolution achievable with microwave Fourier transform spectroscopy. The  $^{14}\text{N}$  quadrupole hyperfine structure of  $\text{NH}_3$  has been fully resolved, and all the coupling constants have been evaluated. The transitions, especially the  $6_{15}-16_{16}$  transition in Fig. 2, are some of the most complex thus far observed and accounted for by this technique. It is still nevertheless the case that assignment of quantum numbers to such transitions is very difficult, if not impossible, without some reasonable prior knowledge of the coupling constants. These are still best obtained by simplifying the spectrum with isotopic substitutions of the type described in this paper.

Table 5 contains a comparison of the measured coupling constants with those measured previously, with those obtained in several *ab initio* predictions, and with those of the two other azides whose  $^{14}\text{N}$  coupling constants are all known. The two constants measured previously by Forman and Lide [1] are in excellent agreement with those measured here, though the precision in the present work is very much better.

There are two sets of *a priori* predictions of the  $^{14}\text{N}$  coupling constants, by Palmer [4], and by Murgich and Aray [5]. Palmer's constants are given in the principal inertial axis system, and a direct comparison can be made with the experimental values. There is clearly good agreement for  $\text{N}_x$ ; it is slightly less good for  $\text{N}_y$ . For the central atom,  $\text{N}_\beta$ , the agreement is fairly poor for  $\chi_{bb}$  and  $\chi_{cc}$ . Murgich and Aray unfortunately do not state their axis systems precisely, and since the constants are often sensitive functions of angle there is little point in making a detailed comparison. However, because of the plane of symmetry the  $\chi_{cc}$  components can be compared. In this case there is

Table 5. Comparison of experimental  $^{14}\text{N}$  nuclear quadrupole constants of  $\text{HN}_3$  with *ab initio* values and with those of other azides.

	$\text{N}_z$			$\text{N}_\beta$			$\text{N}_\gamma$		
	$\chi_{aa}$	$\chi_{bb}$	$\chi_{cc}$	$\chi_{aa}$	$\chi_{bb}$	$\chi_{cc}$	$\chi_{aa}$	$\chi_{bb}$	$\chi_{cc}$
Obs. <sup>a</sup>	4.727 (5)	−1.228 (3)	−3.499 (3)	−0.84 (3)	0.52 (2)	0.32 (2)	−1.224 (14)	2.611 (7)	−1.387 (7)
Obs. <sup>b</sup>	4.85 (10)			<0.7 <sup>c</sup>			−1.35 (10)		
Calc. <sup>d</sup>	4.249	−1.653	−2.596	−0.768	−0.223	0.992	−0.758	2.708	−1.950
Calc. <sup>e</sup>			−1.722			0.122			3.055
Calc. <sup>f</sup>			−1.884			0.302			3.310
$\text{CH}_3\text{N}_3^{\text{g},\text{i}}$	4.744 (4)	−1.354 (2)	−3.390 (4)	−0.950 (5)	0.768 (3)	0.182 (6)	−0.585 (8)	2.259 (4)	−1.674 (9)
$\text{NCN}_3^{\text{h},\text{i}}$	4.82 (2)	−0.70 (8)	−4.12 (10)	−0.85 (7)	0.70 (8)	0.15 (15)	−0.75 (7)	1.55 (5)	−0.80 (12)

<sup>a</sup> Present work.<sup>b</sup> Ref. [1].<sup>c</sup> This is an upper bound to the absolute value of  $\chi_{aa}$ .<sup>d</sup> Palmer, Ref. [4].<sup>e</sup> Ref. [5], 6–31 G\*\* calculations.<sup>f</sup> Ref. [5], Dunning polarization.<sup>g</sup> Ref. [17].<sup>h</sup> Ref. [18].<sup>i</sup> Comparison of values of  $\chi_{aa}$  and  $\chi_{bb}$  amongst the different azides is not entirely valid because the *a*- and *b*-inertial axes are rotated from molecule to molecule.Table 6. Comparison of present and previously reported rotational constants (MHz) of  $\text{H}^{15}\text{N}^{14}\text{N}^{14}\text{N}$  and  $\text{H}^{14}\text{N}^{14}\text{N}^{15}\text{N}$ .

		$\text{H}^{15}\text{N}^{14}\text{N}^{14}\text{N}$	$\text{H}^{14}\text{N}^{14}\text{N}^{15}\text{N}$
<i>A</i>	present work	605 583.30 (15)	610 979.7 (2)
	Ref. [5]	605 378.1 <sup>a</sup>	610 931.1
	Ref. [2]	619 916	616 868
<i>B</i>	present work	11 667.5433 (15)	11 641.7764 (14)
	Ref. [2]	11 667.54	11 641.76
<i>C</i>	present work	11 427.8558 (15)	11 405.0788 (14)
	Ref. [2]	11 427.86	11 405.08

<sup>a</sup> For the previously measured constants the figures given here are those of the original authors. The implied uncertainties of the *A* constants are too small (see text).

moderately good agreement for  $\text{N}_\beta$ , and poor agreement for  $\text{N}_z$ . There is a total disagreement for  $\text{N}_\gamma$ ; it is not clear why this should be so. The same problem was found for both  $\text{CH}_3\text{N}_3$  [17] and  $\text{NCN}_3$  [18]. However Murgich and Aray state strongly that the *z*-principal quadrupole axis is essentially perpendicular to the  $\text{N}_\beta$ – $\text{N}_\gamma$  internuclear axis. If they have interchanged the *z*- and *y*-axes much of the disagreement would be removed.

In comparing the experimental constants of  $\text{HN}_3$  with those of  $\text{CH}_3\text{N}_3$  and  $\text{NCN}_3$ , also in Table 5, one must remember that the angles between the NN axes and the inertial axes vary from molecule to molecule. Again the only really valid comparison is between the  $\chi_{cc}$  values. It would seem that although there are some variations, they are relatively minor.

In Table 6 there is a comparison of the present and earlier rotational constants of the two  $^{15}\text{N}$  isotopomers. For the constants *B* and *C* there is essentially precise agreement, which is hardly surprising since the constants of the present work depend largely on the data of [2]. The precision reported here cannot be considered absolute, since it is dependent on the model used in fitting to the rotational and distortion constants. What is encouraging, however, is that the fits to the rotational constants included the *b*-type transitions; the fact that *B* and *C* do not change is a strong confirmation of the assignment of the lines.

The value of  $d_1$  of the two substituted species was obtained almost entirely from the *a*-type Q-branches measured here. They agree well between themselves, and moderately well with  $\delta_J$  of the normal species [3]. The improved precision in the present work is probably a reflection of the improved accuracy of MWFT over Stark modulated spectroscopy.

For the *A* constants the agreement between the present values and those of [7] can be considered something of a triumph. The latter were obtained by assuming that the inertial defects of all H-containing isotopic species should be equal. Comparison with isoelectronic  $\text{HNCO}$  [15, 19] confirms this assumption, but gives an estimated uncertainty in *A* of  $\pm 300$  MHz. In this limit there is agreement between the two sets of constants. Even more to the point is that Winnewisser [7] used her constants to estimate the structure of  $\text{HN}_3$ . Our results confirm that structure.

### Acknowledgements

We thank Marcello Andolfatto for preparing the samples and Kirsten Vormann for assistance with some of the measurements. Correspondence with M. H. Palmer is also gratefully acknowledged.

This work was supported by the Deutsche Forschungsgemeinschaft, the Land Schleswig-Holstein and the Fonds der Chemie. M.C.L.G. thanks espe-

cially Prof. H. Dreizler and the members of the Abteilung Chemische Physik im Institut für Physikalische Chemie der Universität Kiel for their support, assistance and hospitality during his stay in Kiel. He thanks further the Deutsche Forschungsgemeinschaft for their Guest Professorship. Some computer calculations were carried out at the Rechenzentrum der Universität Kiel.

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